### Advanced Computer Graphics (Fall 2009)

CS 294, Rendering Lecture 10

Precomputation-Based Real-Time Rendering

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### Motivation

- Previously: seen IBR. Use measured data (real photographs) and interpolate for realistic real-time
- Why not apply to real-time rendering?
  - Precompute (offline) some information (images) of interest
  - Must assume something about scene is constant to do so
     Thereafter real-time rendering. Often accelerate hardware
- Easier and harder than conventional IBR
- Easier because synthetic scenes give info re geometry,
- reflectance (but CG rendering often longer than nature)
- Harder because of more complex effects (lighting from all
- directions for instance, not just changing view)

  Representations and Signal-Processing crucial

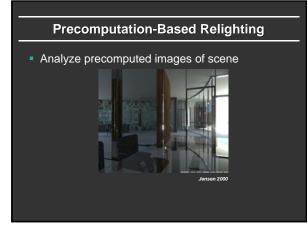
## **My General Philosophy**

- This general line of work is a large data management and signal-processing problem
- Precompute high-dimensional complex data
- Store efficiently (find right mathematical represent.)
- Render in real-time
  - Worry about systems issues like caching
  - Good signal-processing: use only small amount of data but guarantee high fidelity
- Many insights into structure of lighting, BRDFs, ...
   Not just blind interpolation and IBR, signal processing

### **Precomputation-Based Relighting**

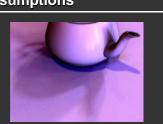
Analyze precomputed images of scene





### Assumptions

- Static geometry
- Precomputation

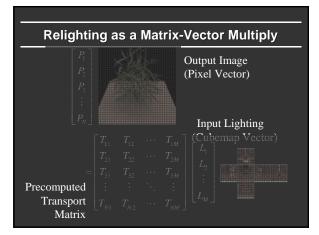


- Real-Time Rendering (relight all-frequency effects)
  - Exploit linearity of light transport for this
  - Later, change viewpoint as well

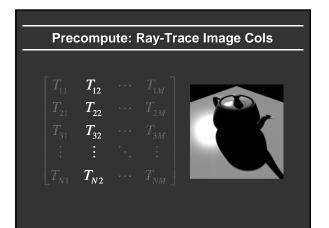
# Why is This Hard?

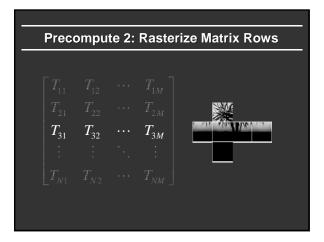
- Plain graphics hardware supports only simple (point) lights, BRDFs (Phong) without any shadows
- Shadow maps can handle point lights (hard shadows)
- Environment maps complex lighting, BRDFs but no shadows
- IBR can often do changing view, fixed lighting
- How to do complex shadows in complex lighting?
- With dynamically changing illumination and view?

Relighting as a Matrix-Vector Multiply $\begin{bmatrix} P_1 \\ P_2 \\ P_3 \\ \vdots \\ P_N \end{bmatrix}$  $\begin{bmatrix} T_{11} & T_{12} & \cdots & T_{1M} \\ T_{21} & T_{22} & \cdots & T_{2M} \\ T_{31} & T_{32} & \cdots & T_{3M} \\ \vdots & \vdots & \ddots & \vdots \\ T_{N1} & T_{N2} & \cdots & T_{NM} \end{bmatrix}$ 



| Matrix Columns (Images) |  |  |  |  |  |
|-------------------------|--|--|--|--|--|
|                         | $T_{12}$<br>$T_{22}$<br>$T_{32}$<br>$\vdots$<br>$T_{N2}$ |  | $ \begin{bmatrix} T_{1M} \\ T_{2M} \\ T_{3M} \\ \vdots \\ T_{NM} \end{bmatrix} $ |  |  |





## **Problem Definition**

#### Matrix is Enormous

- 512 x 512 pixel images
- 6 x 64 x 64 cubemap environments

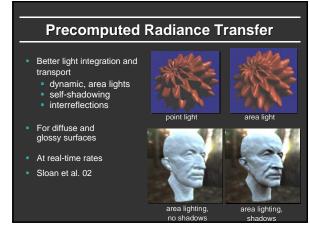
Full matrix-vector multiplication is intractable

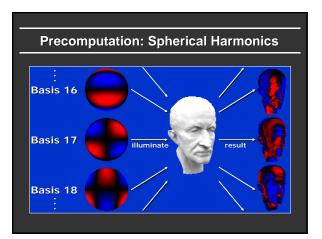
• On the order of 10<sup>10</sup> operations *per frame* 

How to relight quickly?

## Outline

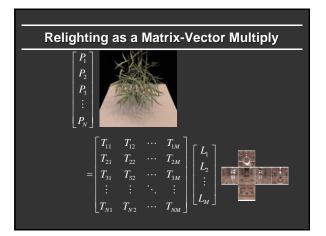
- Motivation and Background
- Compression methods
  - Low frequency linear spherical harmonic approximation
  - Factorization and PCA
  - Local factorization and clustered PCA
  - Non-linear wavelet approximation
- Changing view as well as lighting
  - Clustered PCA
  - Factored BRDFs
  - Triple Product Integrals









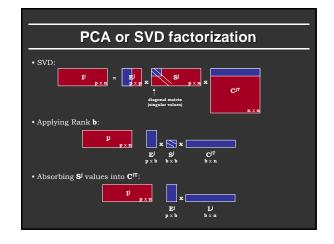


### **Idea of Compression**

- The vector is projected onto low-frequency components (say 25). Size greatly reduced.
- Hence, only 25 matrix columns
- But each pixel still treated separately (still have 300000 matrix rows for 512 x 512 image)
- Actually, for each pixel, dot product of matrix row (25) elems) and lighting vector (25 elems) in hardware
- Good technique (becoming common in games) but useful only for broad low-frequency lighting

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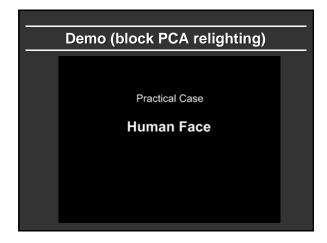


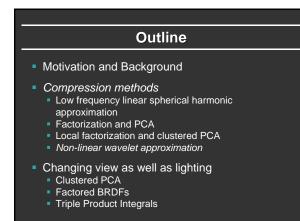
#### Idea of Compression

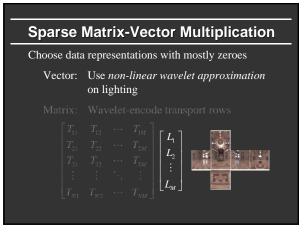
- Represent matrix (rather than light vector) compactly
- Can be (and is) combined with low frequency vector
- Useful in broad contexts.
  - BRDF factorization for real-time rendering (reduce 4D BRDF to 2D texture maps) McCool et al. 01 etc Surface Light field factorization for real-time rendering (4D to 2D
  - maps) Chen et al. 02, Nishino et al. 01
  - Factorization of Orientation Light field for complex lighting and BRDFs (4D to 2D) Latta et al. 02
- Not too useful for general precomput. relighting Transport matrix not low-dimensional!!

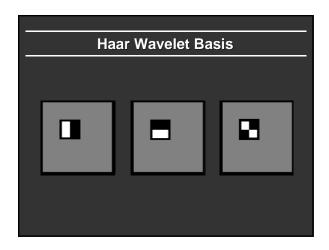
### Local or Clustered PCA

- Exploit local coherence (in say 16x16 pixel blocks)
  - Idea: light transport is locally low-dimensional. Why?
  - Even though globally complexSee Mahajan et al. 07 for theoretical analysis
- Original idea: Each triangle separately
  - Example: Surface Light Fields 3D subspace works well Vague analysis of size of triangles
  - Instead of triangle, 16x16 image blocks [Nayar et al. 04]
- Clustered PCA [Sloan et al. 2003]
  - Combines two widely used compression techniques: Vector Quantization or VQ and Principal Component Analysis
     For complex geometry, no need for parameterization / topology









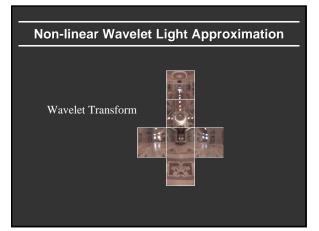
### **Non-linear Wavelet Approximation**

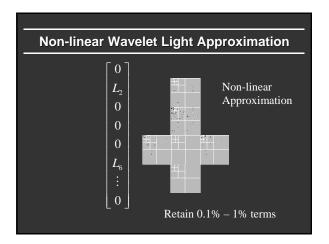
#### Wavelets provide dual space / frequency locality

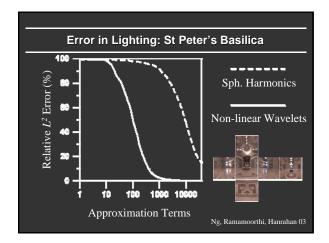
- Large wavelets capture low frequency area lighting
- Small wavelets capture high frequency compact features

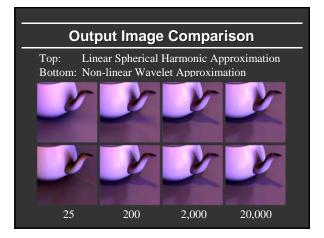
#### Non-linear Approximation

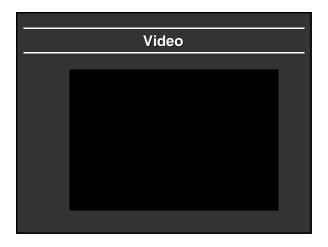
- Use a dynamic set of approximating functions (depends on each frame's lighting)
- By contrast, linear approx. uses fixed set of basis
- functions (like 25 lowest frequency spherical harmonics)We choose 10's 100's from a basis of 24,576 wavelets





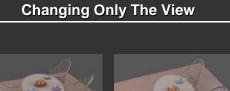


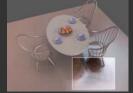




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### **Problem Characterization**

(2D)

**6D** Precomputation Space

- Distant Lighting (2D)
- View
- Rigid Geometry (2D)



With ~ 100 samples per dimension ~ 10<sup>12</sup> samples total!! : Intractable computation, rendering

### **Clustered PCA**

- Use low-frequency light and view variation (Order 4 spherical harmonic = 25 for both; total = 25\*25=625)
- 625 element vector for each vertex
- Apply CPCA directly (Sloan et al. 2003)
- Does not easily scale to high frequencies
   Really cubic complexity (number of vertices, illumination directions or harmonics, and view directions or harmonics)
- Practical real-time method on GPU

### **Factored BRDFs**

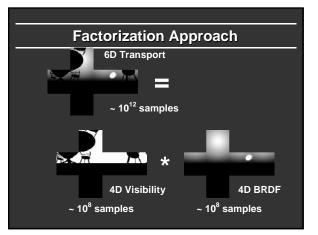
- Sloan et al. 04, Wang et al. 04: All-frequency effects
- Combines lots of things: BRDF factorization, CPCA, nonlinear approx. with wavelets
- Idea: Factor BRDF to depend on incident, outgoing
  - Incident part handled with view-independent relighting
  - Then linearly combine based on outgoing factor
- Effectively, break problem into a few subproblems that can be solved view-independently and added up
  - Can apply nonlinear wavelet approx. to each subproblem
  - And CPCA to the matrices for further compression

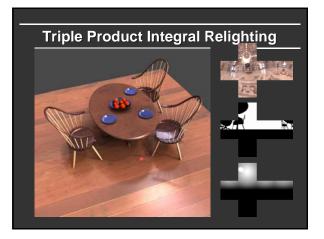
### **Factored BRDFs: Critique**

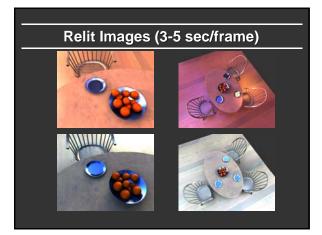
- Simple, reasonably practical method
- Problem: Non-optimal factorization, few terms
   Can only handle less glossy materials
  - Accuracy not properly investigated
- Very nice synthesis of many existing ideas
- Comparison to triple product integrals
  - Not as deep or cool, but simpler and real-time
  - Limits BRDF fidelity, glossiness much more
  - In a sense, they are different types of factorizations

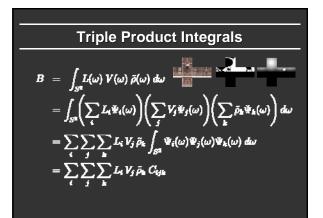
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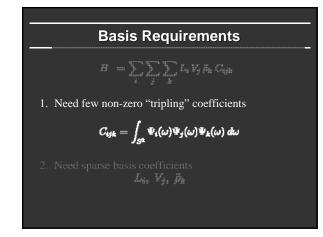
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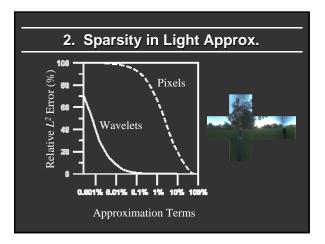








| 1. Number Non-Zero Tripling Coeffs   |                           |  |  |  |  |
|--|---------------------------|--|--|--|--|
| $C_{ijk} = \int_{{m g}^2} \Psi_i(\omega) \Psi_j(\omega) \Psi_k(\omega) \; d\omega$ |                           |  |  |  |  |
| Basis Choice   | Number Non-Zero $C_{ijk}$ |  |  |  |  |
| General (e.g. PCA)   | $O(N^3)$                  |  |  |  |  |
| Pixels   | O(N)                      |  |  |  |  |
| Fourier Series   | $O(N^2)$                  |  |  |  |  |
| Sph. Harmonics   | $O(N^{5/2})$              |  |  |  |  |
| Haar Wavelets  | Q (37 3 37)               |  |  |  |  |



### **Summary of Wavelet Results**

- Derive direct O(N log N) triple product algorithm
- Dynamic programming can eliminate *log N* term
- Final complexity linear in number of retained basis coefficients

### **Broader Computational Relevance**

- Clebsch-Gordan triple product series for spherical harmonics in quantum mechanics (but not focused on computation)
- Essentially no previous work graphics, applied math
- Same machinery applies to basic operation: multiplication
- Signal multiplication for audio, image compositing,....
   Compressed signals/videos (e.g. wavelets JPEG 2000)



## Summary

- Really a big data compression and signalprocessing problem
- Apply many standard methods
   PCA, wavelet, spherical harmonic, factor compression
- And invent new ones
   VQPCA, wavelet triple products
- Guided by and gives insights into properties of illumination, reflectance, visibility
  - How many terms enough? How much sparsity?

## Subsequent Work

- My survey linked from website (lecture only covers 2002-2004)
- Varied lighting/view. What about dynamic scenes, BRDFs
   Much recent work [Zhou et al. 05, Ben-Artzi et al. 06]. But still limited for dynamic scenes
- Must work on GPU to be practical
- Sampling on object geometry remains a challenge
- Near-Field Lighting has had some work, remains a challenge
- Applications to lighting design, direct to indirect transfer
   New basis functions and theory
- Newer methods do not require precompute, various GPU tricks
- So far, low-frequency spherical harmonics used in games, all-frequency techniques have had limited applicability