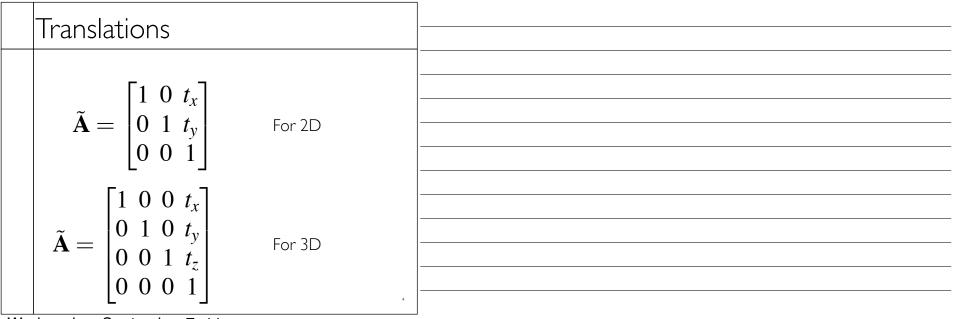
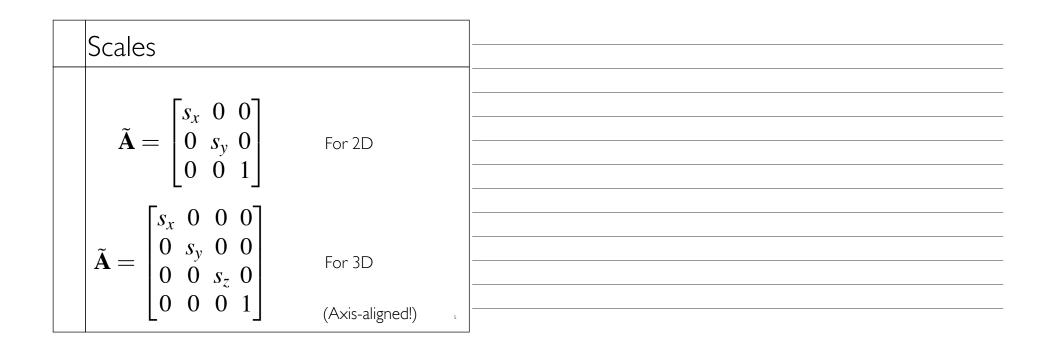
CS-184: Computer Graphics	
Lecture #5: 3D Transformations and Rotations	
Prof. James O'Brien University of California, Berkeley	

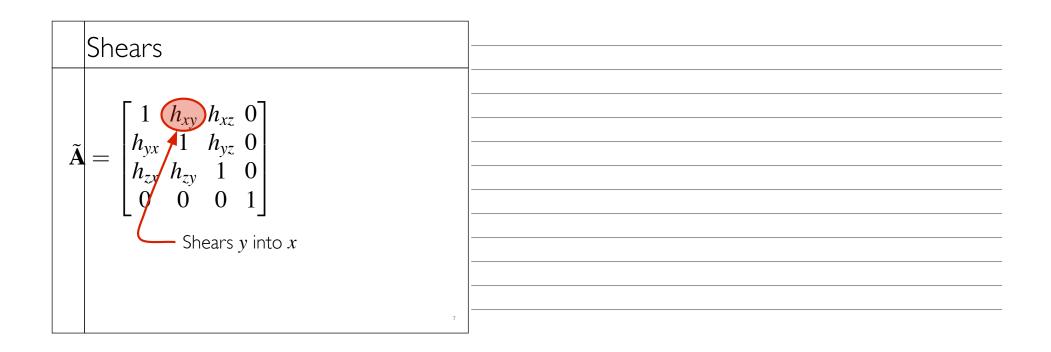
Today	
Transformations in 3DRotations	
 • Rotations • Matrices • Euler angles 	
Exponential mapsQuaternions	
2	

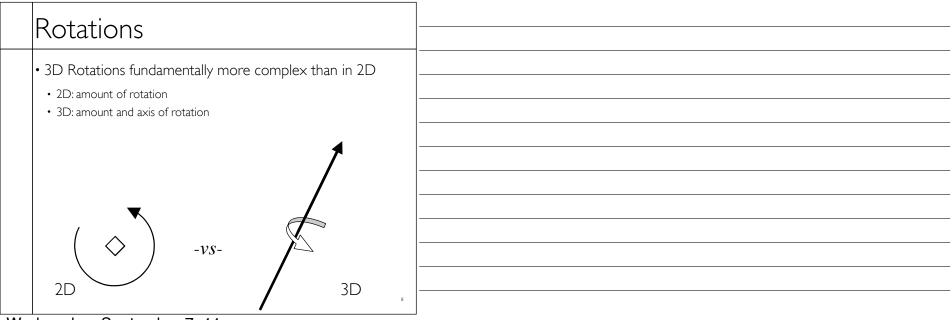
3D Transformations
• Generally, the extension from 2D to 3D is straightforward
Vectors get longer by oneMatrices get extra column and row
 SVD still works the same way Scale, Translation, and Shear all basically the same
Rotations get interesting
3

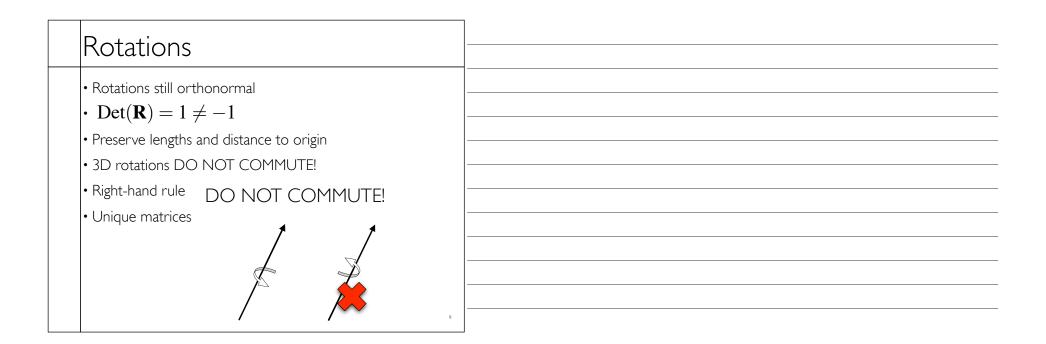


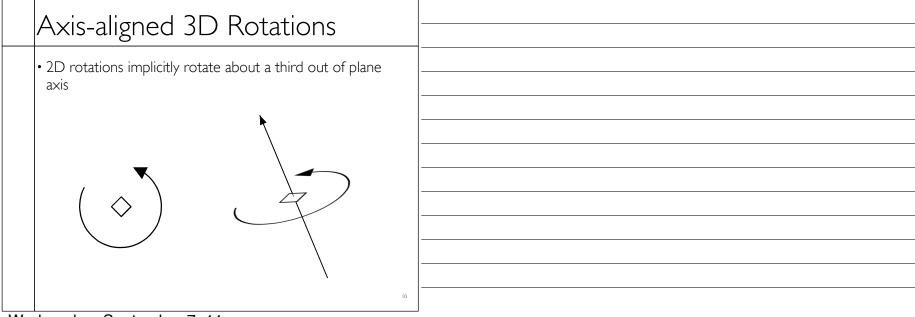


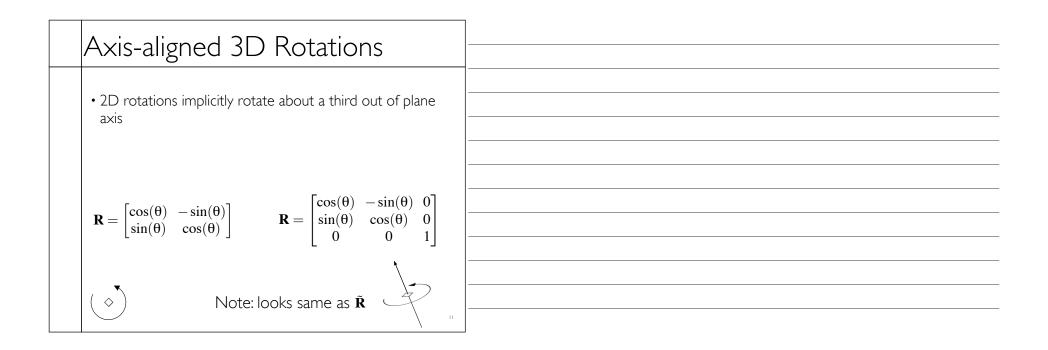


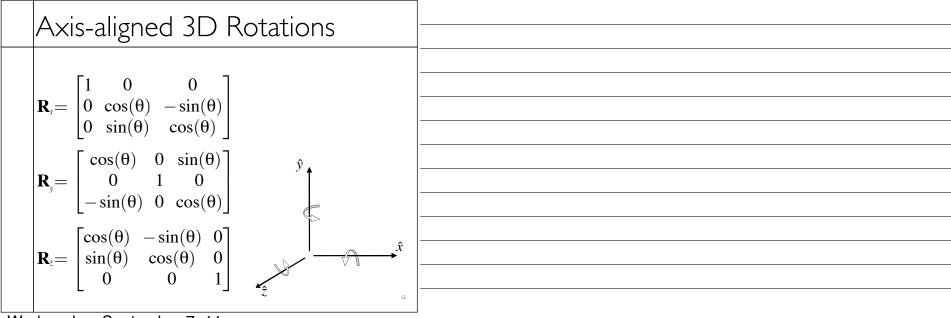


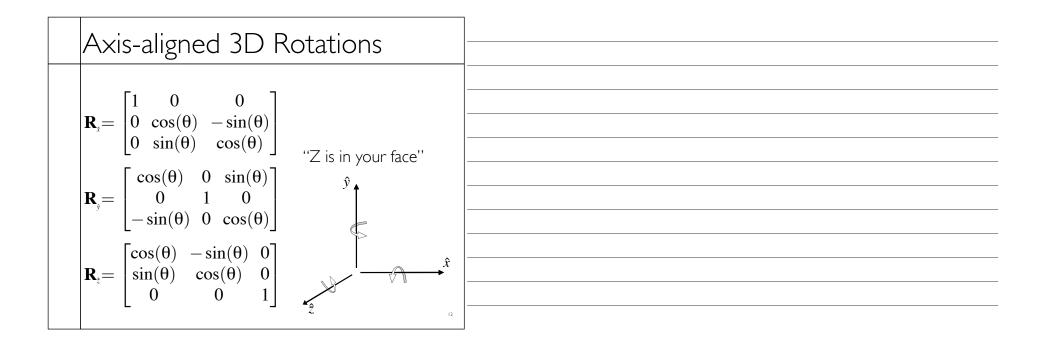


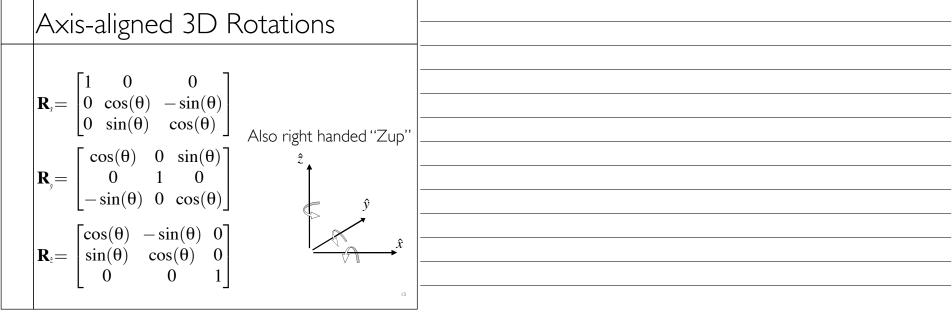


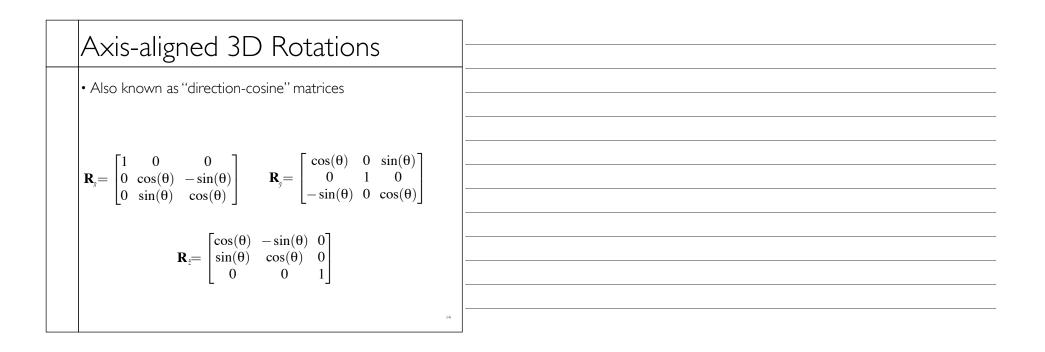


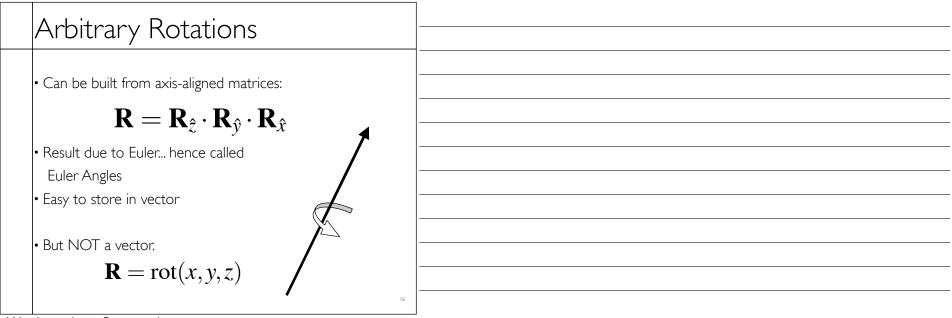


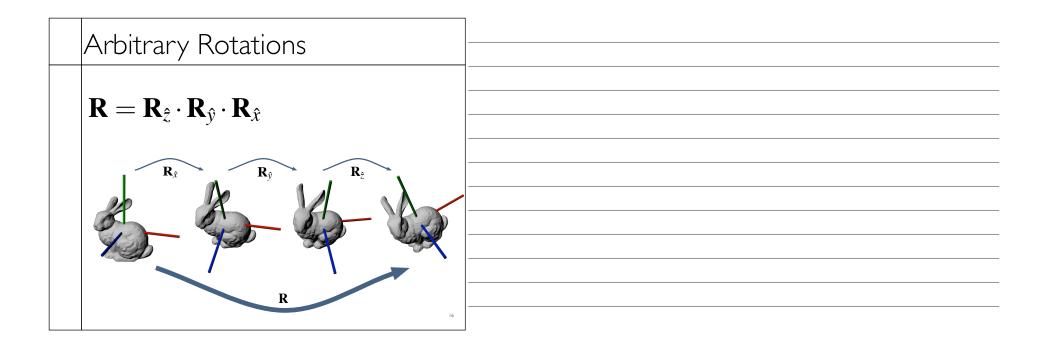


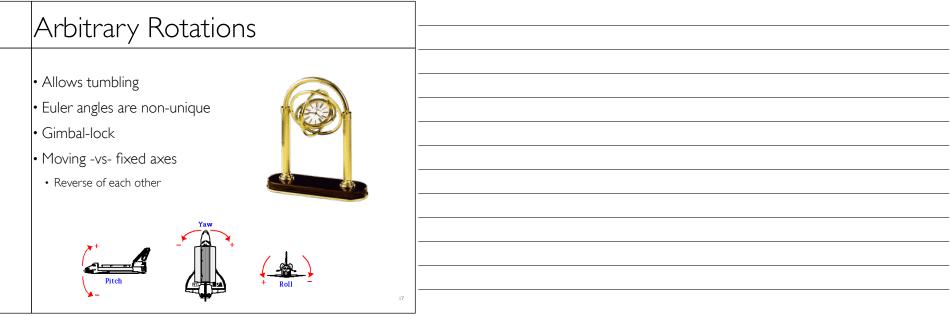


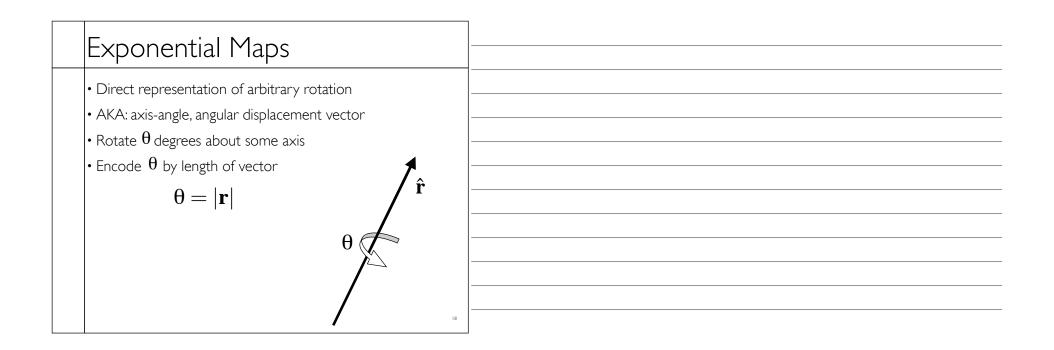


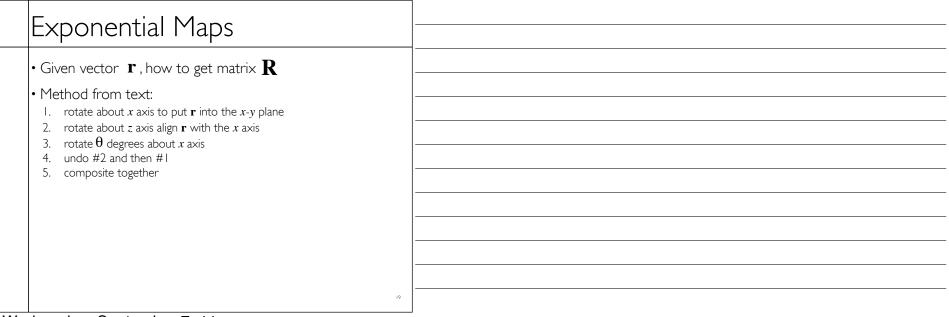


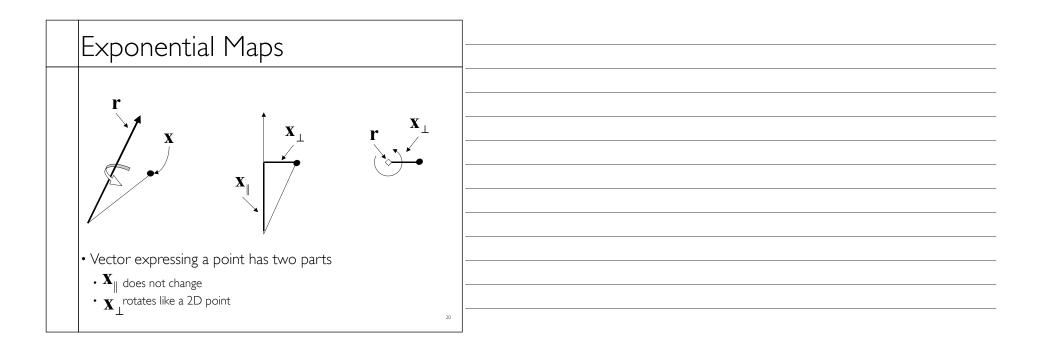


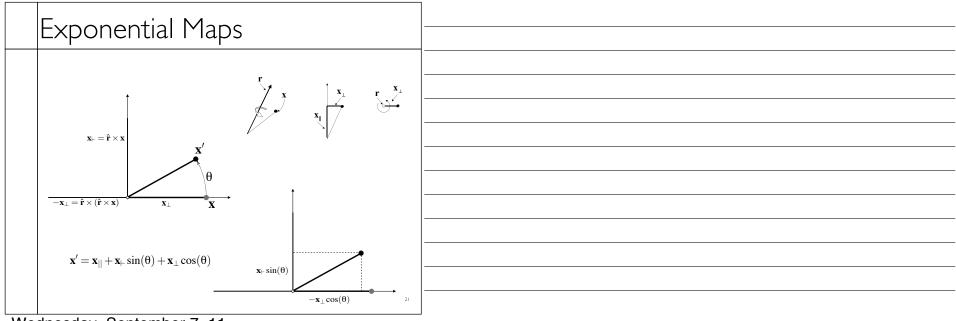


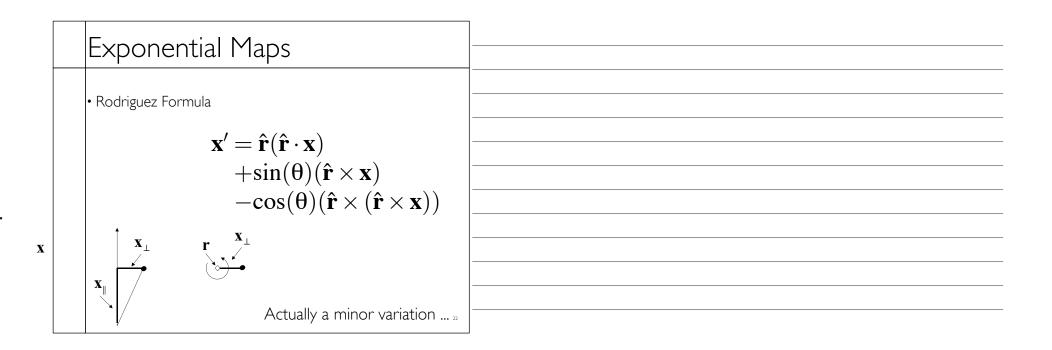


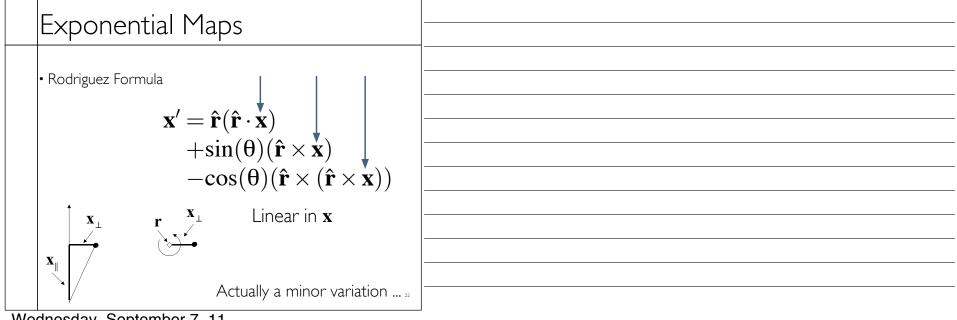




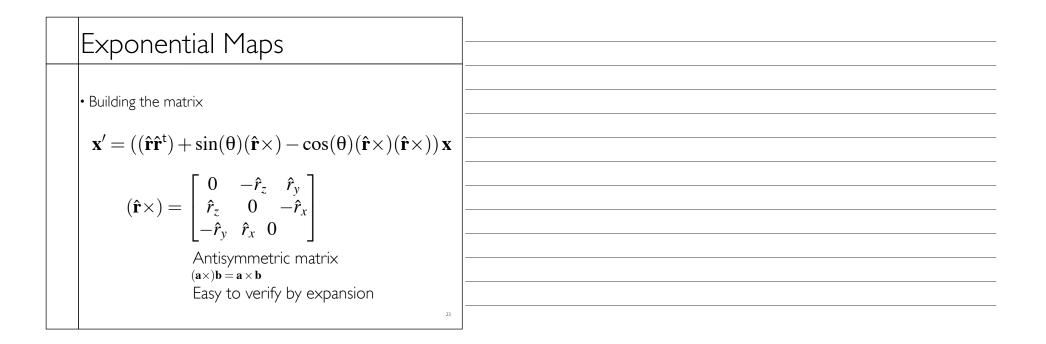




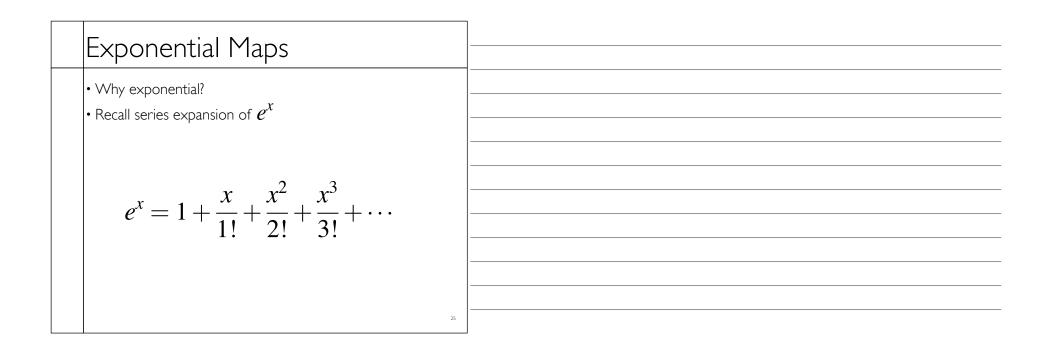


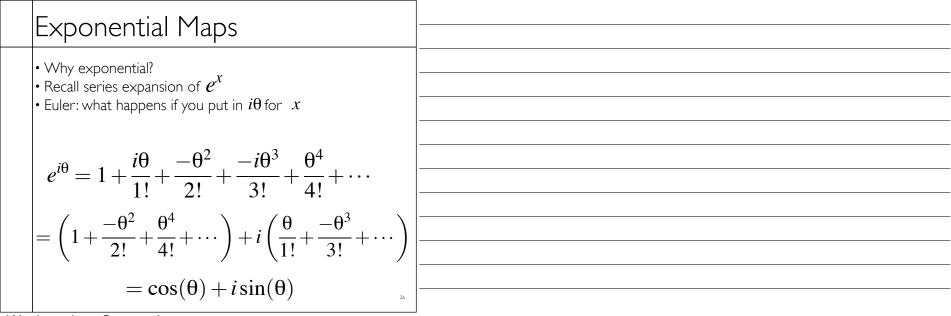


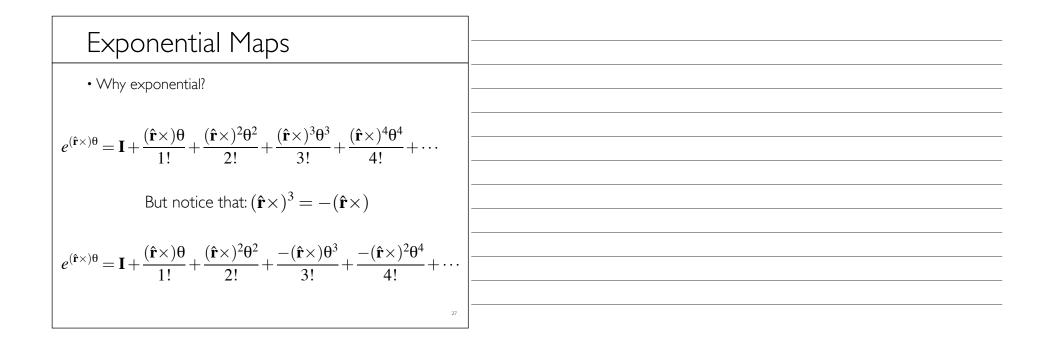
Х

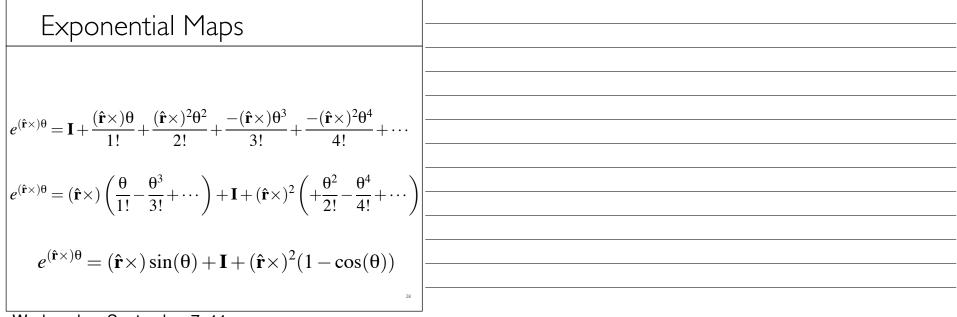


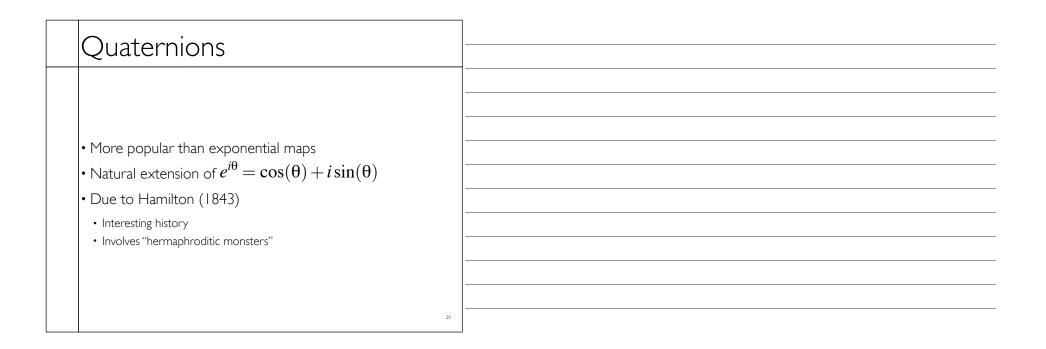
Exponential Maps	
Allows tumbling	
• No gimbal-lock!	
\cdot Orientations are space within π -radius ball	
Nearly unique representation	
\cdot Singularities on shells at 2 π	
Nice for interpolation	
24	



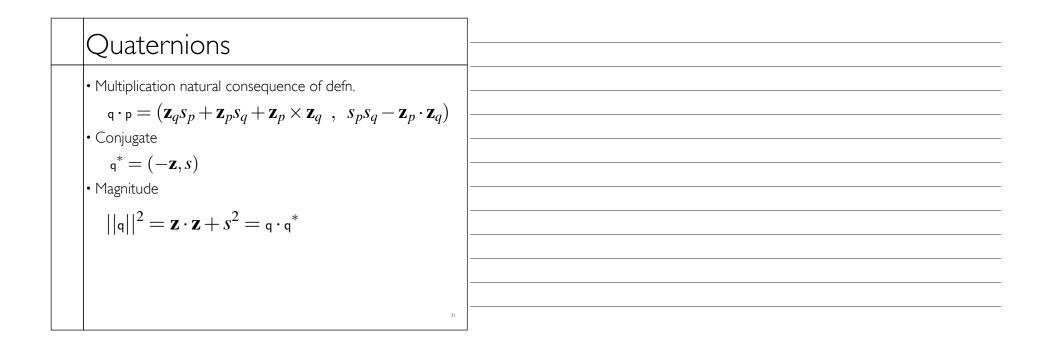


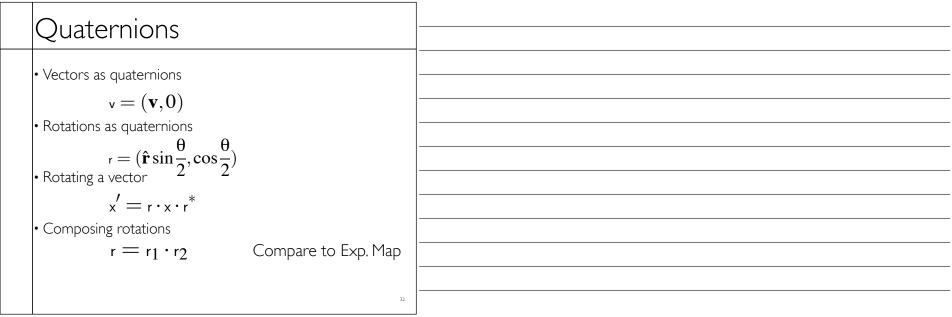


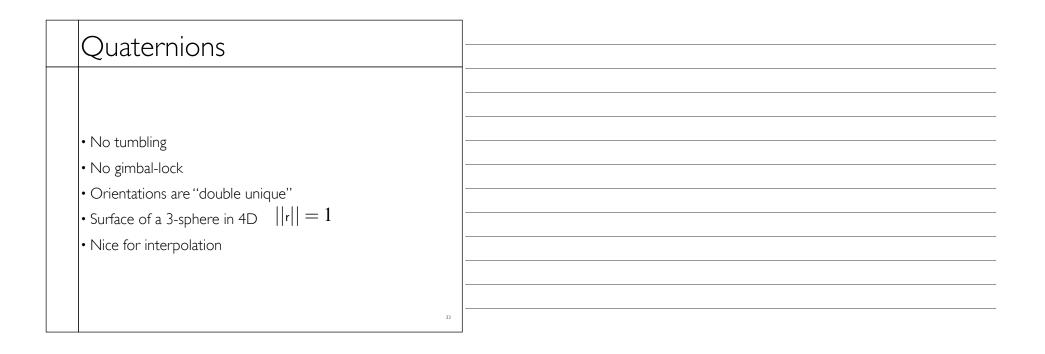


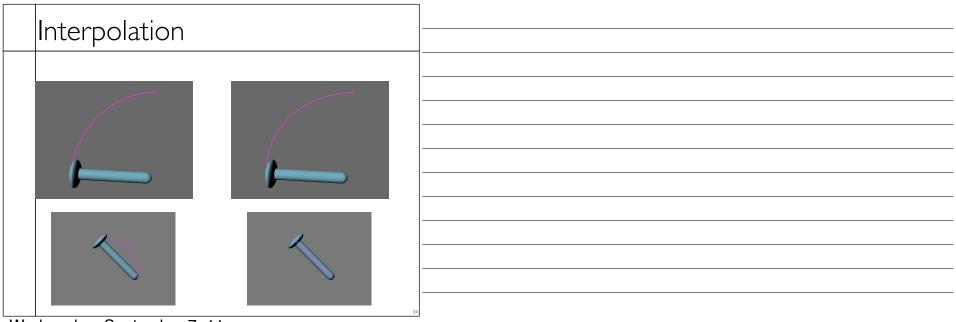


Quaternions]
Uber-Complex Numbers	
q = $(z_1, z_2, z_3, s) = (\mathbf{z}, s)$	
$\mathbf{q} = iz_1 + jz_2 + kz_3 + s$	
ij = k ji = -k $i^2 = j^2 = k^2 = -1 \qquad jk = i kj = -i$	
ki = j ik = -j	

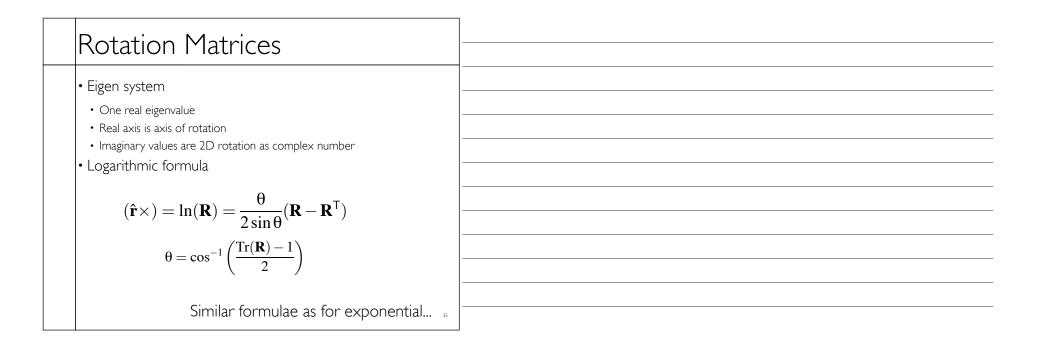


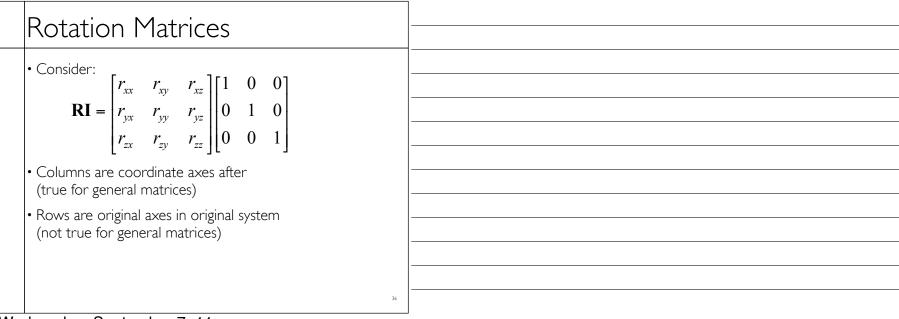


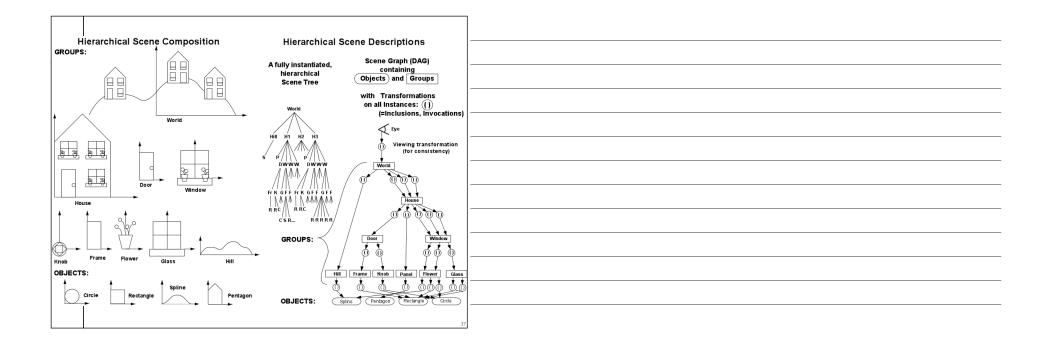




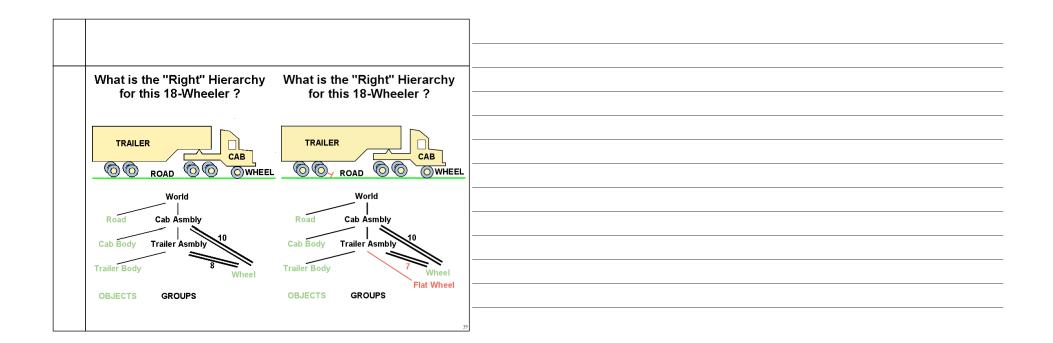
Wednesday, September 7, 11







Scene Graphs
Draw scene with pre-and-post-order traversal
Apply node, draw children, undo node if applicable
• Nodes can do pretty much anything
 Geometry, transformations, groups, color, switch, scripts, etc. Node types are application/implementation specific
Requires a stack to implement "undo" post children
• Nodes can cache their children
 Instances make it a DAG, not strictly a tree
• Will use these trees later for bounding box trees
38



Note:	
• Rotation stuff in the book is a bit weak luckily you have these nice slides!	