

| Today |
| :--- |
|  |
| - The Rendering Equation |
| $\circ$ Radiosity Method |
| $\circ$ Photon Mapping |
| $\circ$ Ambient Occlusion |
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Wednesday, November 5, 2008


## The Rendering Equation

$L_{s}\left(\mathbf{x}, \mathbf{x}^{\prime}\right)=\delta\left(\mathbf{x}, \mathbf{x}^{\prime}\right)\left[E\left(\mathbf{x}, \mathbf{x}^{\prime}\right)+\int_{s^{\prime}} p_{x}\left(\mathbf{x}, \mathbf{x}^{\prime \prime}\right) L_{s}\left(\mathbf{x}^{\prime}, \mathbf{x}^{\prime}\right) \frac{\cos \left(\theta^{\prime}\right) \cos \left(\theta^{\prime \prime}\right)}{\left\|\mathbf{x}^{\prime}-\mathbf{x}^{\prime}\right\|^{2}} \mathbf{d \mathbf { x } ^ { \prime }}\right]$


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| The Rendering Equation |
| :---: |
| $\begin{aligned} L_{s}\left(\mathbf{x}, \mathbf{x}^{\prime}\right)= & \delta\left(\mathbf{x}, \mathbf{x}^{\prime}\right)\left[E\left(\mathbf{x}, \mathbf{x}^{\prime}\right)+\int_{S} \rho_{x^{\prime}}\left(\mathbf{x}, \mathbf{x}^{\prime \prime}\right) L_{s}\left(\mathbf{x}^{\prime}, \mathbf{x}^{\prime \prime}\right) \frac{\cos \left(\theta^{\prime}\right) \cos \left(\theta^{\prime \prime}\right)}{\left\\|\mathbf{x}^{\prime}-\mathbf{x}^{\prime \prime}\right\\|^{2}} \mathrm{~d} \mathbf{x}^{\prime \prime}\right] \\ & \text { sum over every bit of surface in the scene } \end{aligned}$ |


| The Rendering Equation |
| :---: |
| $L_{s}\left(\mathbf{x}, \mathbf{x}^{\prime}\right)=\delta\left(\mathbf{x}, \mathbf{x}^{\prime}\right)\left[E\left(\mathbf{x}, \mathbf{x}^{\prime}\right)+\int_{s^{\prime}} \rho_{x}\left(\mathbf{x}, \mathbf{x}^{\prime \prime}\right) L_{s}\left(\mathbf{x}^{\prime}, \mathbf{x}^{\prime \prime}\right) \cdot \frac{\cos \left(\theta^{\prime}\right) \cos \left(\theta^{\prime \prime}\right)}{\left\\|\mathbf{x}^{\prime}-\mathbf{x}^{\prime \prime}\right\\|^{\prime}} \mathbf{d x}^{\prime} \mathbf{x}^{\prime}\right]$ |

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| Radiosity |
| :--- |
| - Assume all materials are perfectly |
| Lambertian (diffuse only, no specularities) |
| - Removes all dependance on directions |
| - Reduces dimensionality of lighfield |
| - Allows a FEM solution (break up into chunks) |
| - Can also relax assumption slightly... |
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| Radiosity Method |  |
| :---: | :---: |
| - Given the light emitted and surface properties |  |
| - First compute $F_{i j}$, form factors between patches |  |
| - Then solve a linear system to balance energy between all patches |  |
| - Comments: |  |
| - The system is very large |  |
| - It is also sparse (why?) |  |
| - Should be solved with an iterative method - e.g.jacobi or Gauss-Seidel |  |
| - Solution is view independent |  |

## Progressive Radiosity

- If magnitude of eigenvalues of $\mathbf{A}<1$
$(\mathbf{I}-\mathbf{A})^{-1}=\mathbf{I}+\mathbf{A}+\mathbf{A}^{2}+\mathbf{A}^{3}+$
- True for form-factor matrices
$\circ \mathbf{h}^{k+1}=\mathbf{h}^{\mathbf{k}}+\mathbf{u}^{\mathbf{k}+1}$
Idea: let important sources $\mathbf{u}^{k+1}=\mathbf{A u}^{k}$
$\mathbf{h}^{\mathbf{0}}=0 \quad \begin{gathered}\mathbf{u}^{0}=\mathbf{e}\end{gathered} \quad \begin{gathered}\text { of light enerery emit first, } \\ \text { don't even bother with dark things }\end{gathered}$
- Use Gauss-Seidel-like iteration but reorder by
priority



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| Hierarchical Radiosity |
| :--- |
| $\circ$ Light smoothes with distance |
| $\circ$ Compare $1 / h^{2}$ with $1 /\left(h^{2}+d^{2}\right)$ as $h$ gets large |
| $\circ$ Group patches into hierarchy |
| $\circ$ Far interactions use lower-res form factors |

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| Computing Form Factors |  |
| :---: | :---: |
| - Form factors have a geometric meaning |  |
| $11$ |  |
| 为 |  |

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Computing Form Factors
○ Form factors have a geometric meaning
oHemicube" algorithm uses regular scan
conversion

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## Computing Form Factors

- Form factors have a geometric meaning
- "Hemicube" algorithm uses regular scan conversion
- Also computed by ray-based sampling - In practice, computing form factors is the bottleneck24

| Photon Mapping |
| :---: |
| - Lights cast "photons" into environment |
| $\circ$. Cast in random directions |
| $\circ$ Trace into environment |
| $\circ$ Store records at intersections |

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| Photon Mapping |
| :--- |
| 。Final Gather |
| 。 Ray trace scene |
| －Direct and specular rays as normal |
| －Diffuse rays traced into photon map |
| －Diffuse reflection smoothes noise |
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| Ambient Occlusion |
| :--- |
| 。A＂hack＂to create more realistic ambient |
| illumination cheaply |
| －Assume light from everywhere is partially |
| blocked by local objects |
| －Ata point on the surface cast rays at random |
| 。Ambient term is proportional to percent of rays that |
| hit nothing |
| －Weight average by cosine of angle with normal |
| －Take into account how far before occluded |

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Ambient Occlusion

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