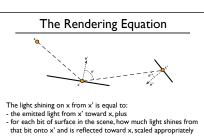
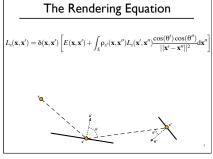
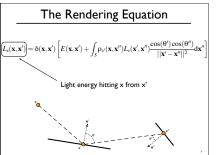
CS-184: Computer Graphics Lecture #16: Global Illumination 1 Today \circ The Rendering Equation • Radiosity Method • Photon Mapping Ambient Occlusion 2 The Rendering Equation The light shining on x from x' is equal to: - the emitted light from x' toward x, plus - for each bit of surface in the scene, how much light shines from that bit onto x' and is reflected toward x, scaled appropriately

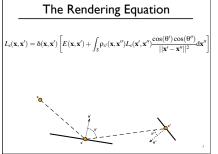


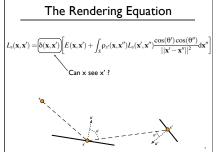
$$L_s(\mathbf{x}, \mathbf{x}') = \delta(\mathbf{x}, \mathbf{x}') \left[E(\mathbf{x}, \mathbf{x}') + \int_{S} \rho_{x'}(\mathbf{x}, \mathbf{x}'') L_s(\mathbf{x}', \mathbf{x}'') \frac{\cos(\theta') \cos(\theta'')}{||\mathbf{x}' - \mathbf{x}''||^2} d\mathbf{x}'' \right]$$

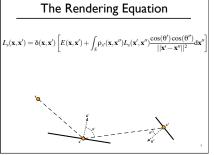


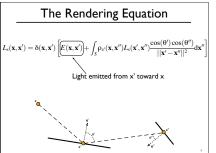


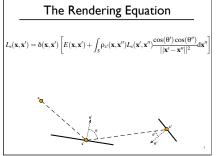


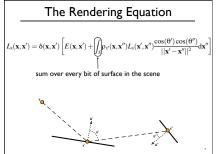


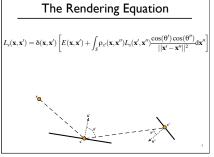


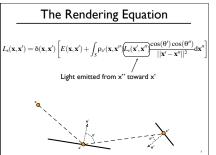


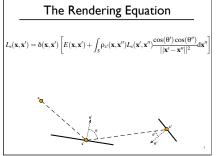


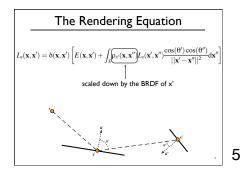


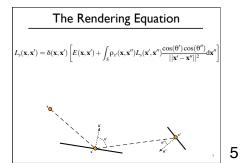


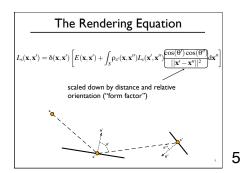


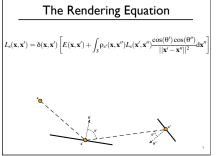












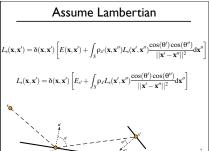
Radiosity

- Assume all materials are perfectly Lambertian (diffuse only, no specularities)
- Removes all dependance on directions
- \circ Reduces dimensionality of lightfield
- · Allows a FEM solution (break up into chunks)
- o Can also relax assumption slightly...

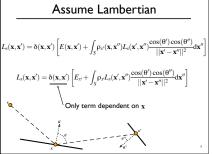


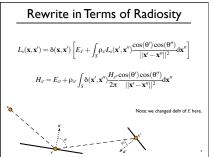


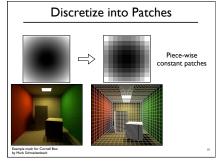
7

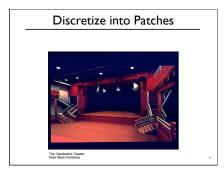


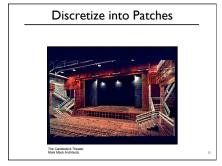
8

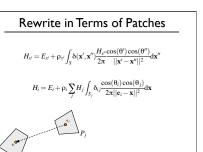


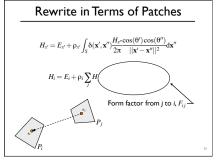




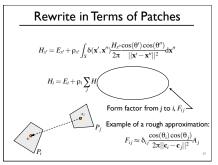








13



13

Radiosity Method

- Given the E_i and ρ_i
- First compute Fij
- Then solve $H_i = E_i + \rho_i \sum H_j F_{ij}$ $(\mathbf{I} \mathbf{A})\mathbf{h} =$
- Comments:
- \circ The matrix \boldsymbol{A} is typically very large
- It is also sparse (why?)
- Should be solved with an iterative method
 e.g.: Jacobi or Gauss-Seidel
- Solution is view independent

Radiosity Method

- Given the light emitted and surface properties
- First compute F_{ij} , form factors between patches
- Then solve a linear system to balance energy between all patches
- Comments:
- \circ The system is very large
- · It is also sparse (why?)
- · Should be solved with an iterative method
- · e.g.: Jacobi or Gauss-Seidel
- Solution is view independent

15

Progressive Radiosity

 \circ If magnitude of eigenvalues of A<1

$$(I - A)^{-1} = I + A + A^2 + A^3 + \cdots$$

- True for form-factor matrices
- $\bullet \ \mathbf{h}^{k+1} = \mathbf{h}^k + \mathbf{u}^{k+1}$ $\mathbf{u}^{k+1} = \mathbf{A} \, \mathbf{u}^k$

Idea: let important sources of light energy emit first, maybe $\mathbf{h}^0 = 0 \quad \mathbf{u}^0 = \mathbf{e}$ don't even bother with dark things

· Use Gauss-Seidel-like iteration but reorder by priority

Southwell Relaxation

16

Progressive Radiosity



17

Touchup

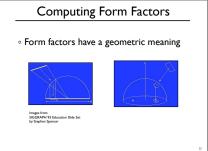
- Each patch will have a constant color
 - \circ Smooth solution (e.g. average to vertices)

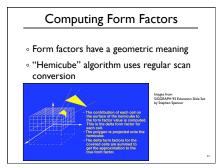




Other Things • Each patch will have a constant color • Smooth solution (e.g. average to vertices) • No specular reflection $_{\circ}$ Add Phong specular term or ray traced specular reflection · Grid artifacts • Be clever with grid... 19 Hierarchical Radiosity • Light smoothes with distance • Compare $1/h^2$ with $1/(h^2+d^2)$ as h gets large 20 Hierarchical Radiosity Light smoothes with distance \circ Compare $1/h^2$ with $1/(h^2+d^2)$ as h gets large • Group patches into hierarchy

• Far interactions use lower-res form factors





Computing Form Factors

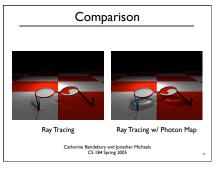
- Form factors have a geometric meaning
- "Hemicube" algorithm uses regular scan conversion
- · Also computed by ray-based sampling
- In practice, computing form factors is the bottleneck

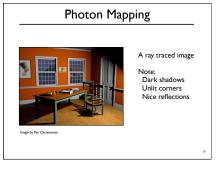
24

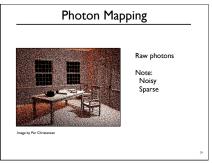
Photon Mapping • Lights cast "photons" into environment • Cast in random directions • Trace into environment • Store records at intersections

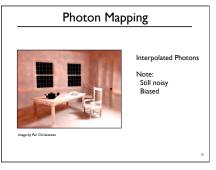
25

Photon Mapping • Lights cast "photons" into environment • Cast in random directions • Trace into environment • Store records at intersections • With KD-Trees...









Photon Mapping Interpolated Photons (multiplied by diffuse) Note: Still noisy Biased

31

Photon Mapping

- Final Gather
- · Ray trace scene
- Direct and specular rays as normal
- · Diffuse rays traced into photon map
- · Diffuse reflection smoothes noise

32

Photon Mapping



Final Image

Note: Not noisy Nice lighting Reflections May still be biased

Final gather often bottleneck...

33

Ambient Occlusion

- A "hack" to create more realistic ambient illumination cheaply
- Assume light from everywhere is partially blocked by local objects
- $\,{\scriptstyle \circ}\,$ At a point on the surface cast rays at random
- \circ Ambient term is proportional to percent of rays that hit nothing
- $\,{}^{_{\odot}}$ Weight average by cosine of angle with normal
- Take into account how far before occluded

