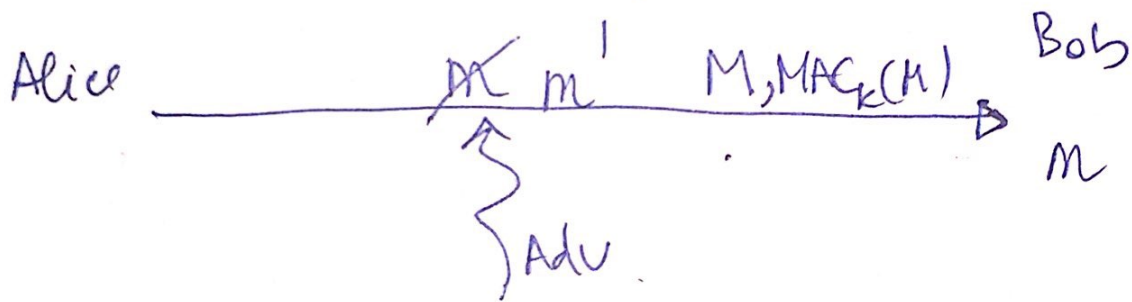


CS/61 Announcements

HW 2 Due Tomorrow

Midterm

Integrity & Authentication



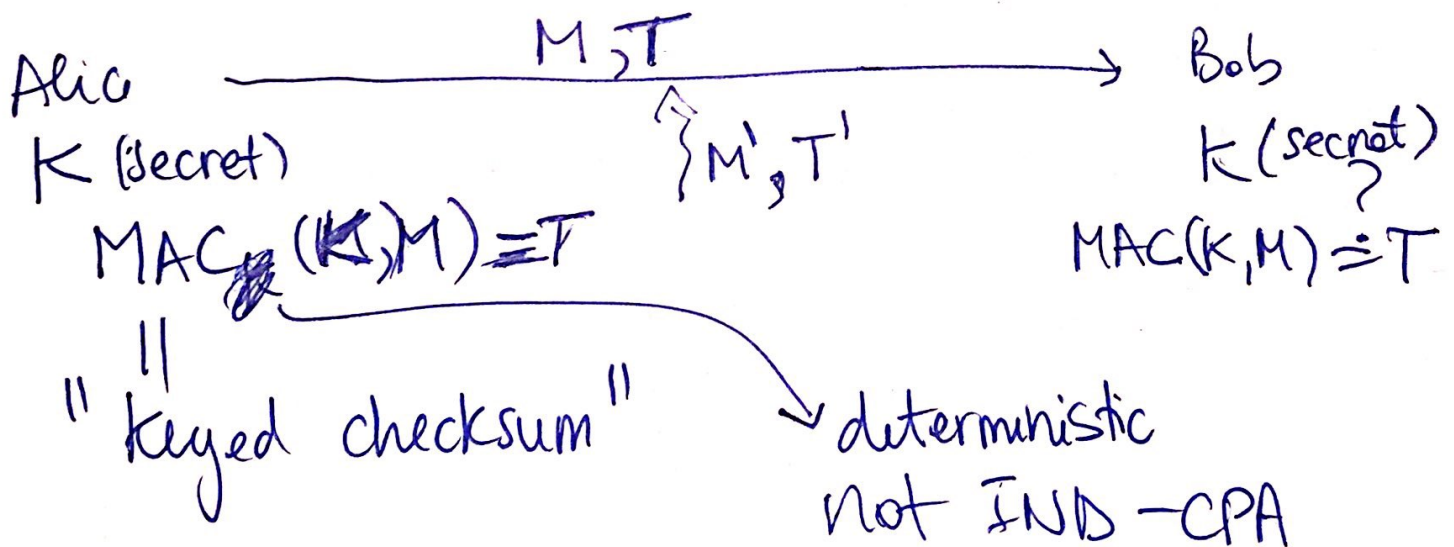
Bob wants to check:

1. authentication: message comes from Alice
2. integrity: message is as sent by Alice (no attacker modified message)

ElGamal cph: $m \cdot (r^a) \pmod p$

	Symmetric-key	Asymmetric-key
Confidentiality	AES-CBC, AES-CTR	El Gamal
Integrity & authentication	MAC	Digital Signatures (RSA)
	Today	

MAC (Message Authentication Code)

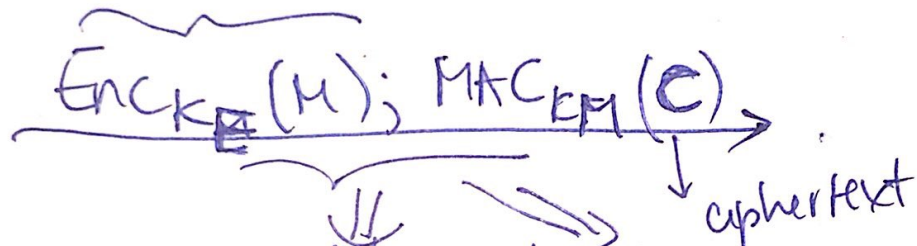
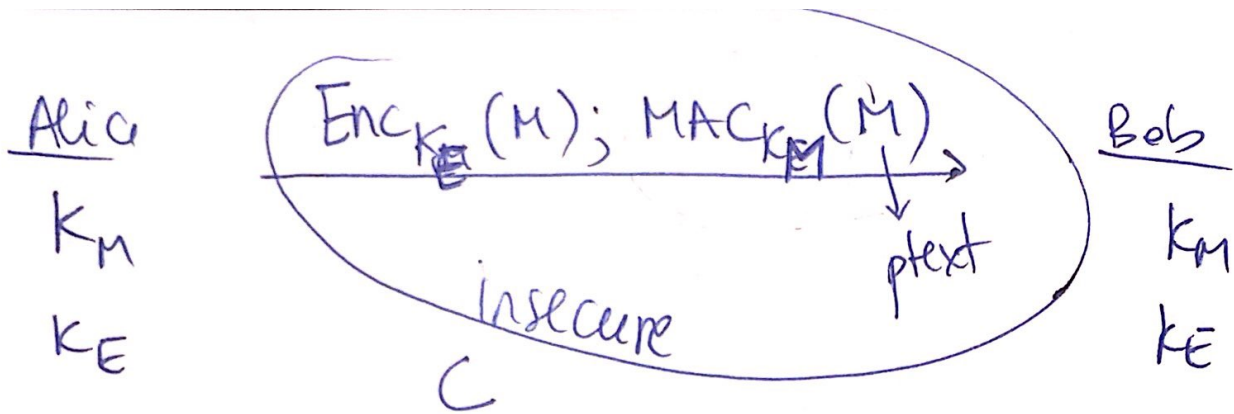


$T \xrightarrow{\text{MAC}_k} M$

Cannot find M' & T' s.t. $\text{MAC}(k, M') = T'$

Existentially unforgeable: Adversary cannot find any pair (M', T') s.t. $\text{MAC}(k, M') = T'$ unless it saw M', T' from a legitimate sender

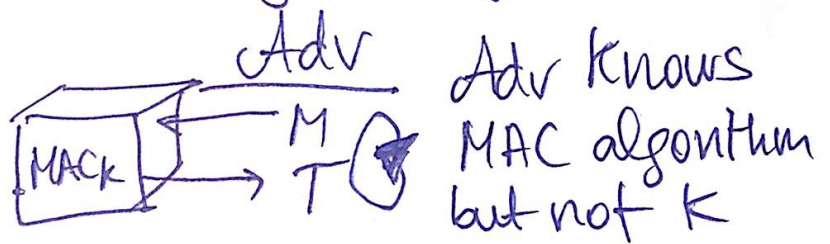
* cannot compute MAC for a new message



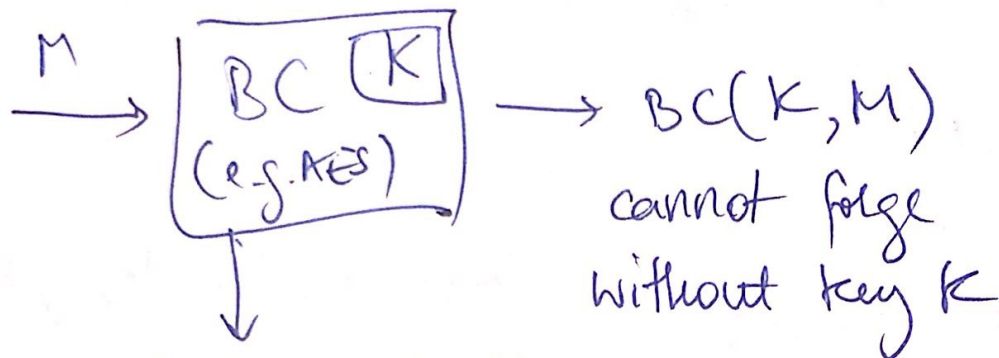
want both confidentiality and integrity

MAC security: existentially unforgeable

$\frac{Ch}{K}$



$$\Pr[\text{Adv}(\cdot) \rightarrow M', T' \text{ s.t. } T' = \text{MAC}_K(M') \ \& \ \text{Adv did not ask for } M' \text{ to MAC Box}] = \text{negl}$$



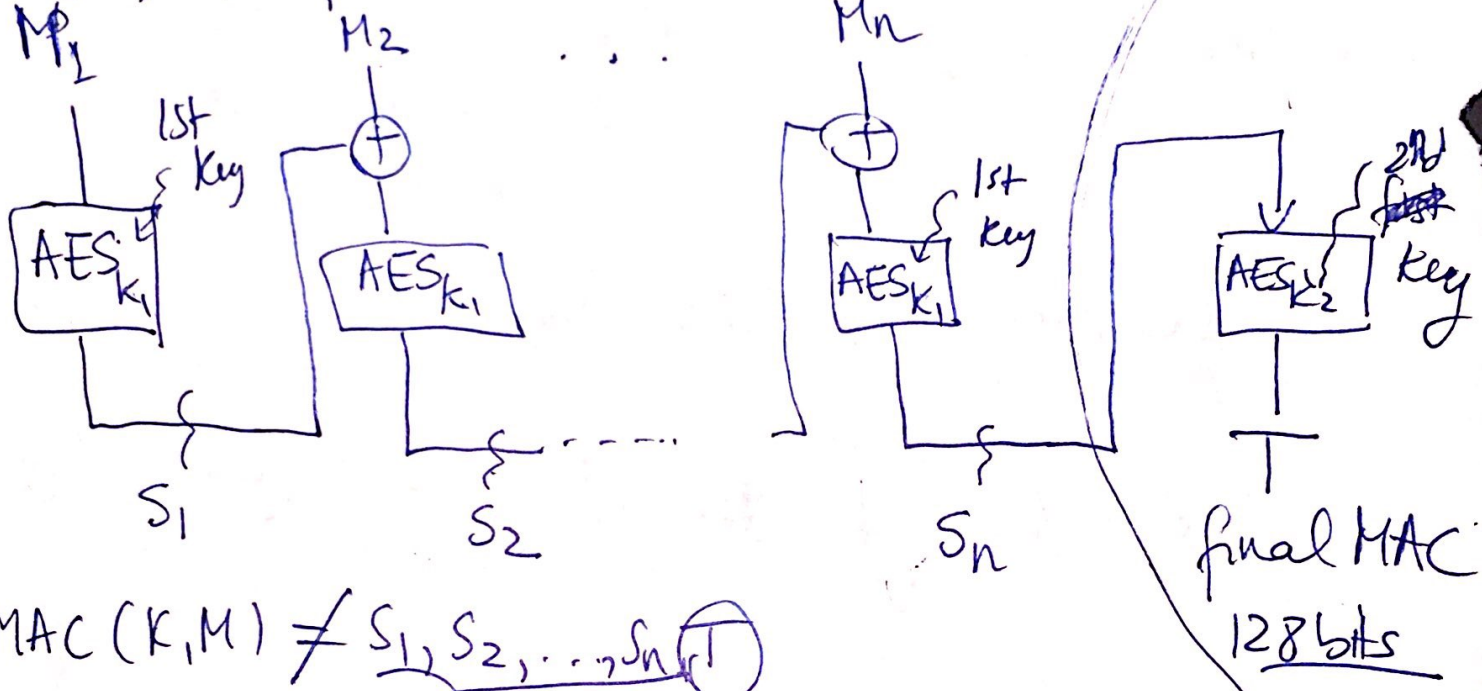
fixed block length
 (e.g. AES has ~~256~~ 128 bits)

$\boxed{\text{AES-EMAC}}$: chaining mode that gives an existentially unforgeable MAC

$K = 256 \text{ bits} = (K_1, K_2) = \text{two AES keys}$

$\text{MAC}(K, M)$: - split M into 128 bit blocks:
 M_1, M_2, \dots, M_n

$$\text{MAC}(K, M) = T$$



$$\text{MAC}(K, M) \neq S_1, S_2, \dots, S_n \text{ (T)}$$

not in MAC ↓ only this is MAC
 because no need to decrypt
 & because receiver can compute
 T without S_1, \dots, S_n

$$\text{MAC}(K, M) = S_n \Rightarrow \text{forgeable}$$

$MAC(k, M_1) = S_1$
 $MAC(k, M_1') = S_1'$
 $MAC(k, \{M_1, M_2\}) = S_2$

} attacker saw this

$MAC(k, [M_1, S_1 \oplus M_2 \oplus S_1']) = S_2$

} happens without k_2
 \Rightarrow why k_2 is needed

forges this

Forgeable $MAC(k, M) = S_n$ forgeable.

plaintext blocks:

M_1, M_2, M_i

$$MAC(k, M_1) = S_1$$

$$MAC(k, M_i) = S_i$$

~~$$MAC(k, (M_1, M_2)) = S_2$$~~

$$MAC(k, (M_1, M_2)) = S_2$$

$$MAC(k, \underbrace{[M_1, \cancel{S_1}, M_2 \oplus S_1]}_{\text{new message}}) = \underline{S_2} \quad ?$$

$$AES_k(M_i) = S_i$$

~~$$S_1 \oplus \cancel{S_1} \oplus M_2 \oplus S_1$$~~

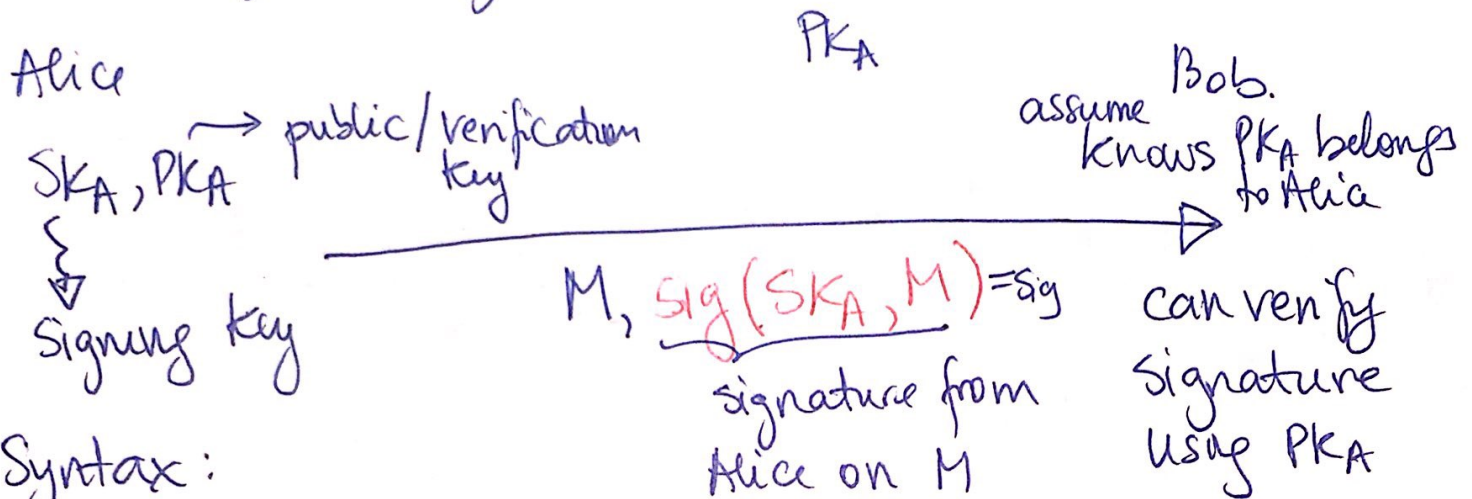
HMAC (K, M) = MAC that is also a hash. function
(collision resistant &
one way)

Construct from hash function

$$H(K \oplus \text{opad} \parallel H(K \oplus \text{ipad} \parallel M))$$

padding 0x5C
repeated

Digital signatures



Syntax:

- 1) $\text{keygen}() \rightarrow (SK, PK)$
- 2) $\text{sign}(SK, m) \rightarrow \text{sig.}$
- 3) $\text{verify}(PK, m, \text{sig}) \rightarrow \%$

No attacker can forge a signature

Existentially unforgeable (same as for MAC) = attacker cannot produce M', sig' s.t. $\text{Verify}(PK, M', \text{sig}') = 1$ (if the attacker did not see M', sig' before)

RSA Signature.

Keygen(): pick random p, q primes 2048 bits
 $p, q \equiv 2 \pmod{3}$ // Keep Secret

$$n = p \cdot q$$

Euler's totient function $\phi(n) = (p-1)(q-1)$

$$x^{\phi(n)} \equiv 1 \pmod{n} \quad (\text{Fermat's Little Theorem})$$

$$\text{PK} = n$$
$$\text{SK} = d$$

secret

Computed s.t.

$$\exists d \equiv 1 \pmod{\phi(n)} \Rightarrow \exists d = \phi(n) \cdot k + 1$$

$$\text{Sign}(\text{SK}, M) =$$

$$\frac{H(M)^d}{\text{sig}} \pmod{n}, \text{ where } H \text{ is Crypto hash}$$

$$\text{Verify}(\text{PK}, M, \text{sig}) \stackrel{?}{=} \text{sig}^3 \pmod{n} \stackrel{?}{=} H(M)$$

$$(H(M)^d)^3 \equiv H(M) \pmod{n}$$

Assumes factoring is hard

Cannot factor n into p & q

Crypto
assumption
RSA